

1 PRINTING A TRUE-INK REFERENCE, AND REFINING GRAY ACCURACY,
2 FOR OPTIMUM COLOR CALIBRATION IN INCREMENTAL PRINTING

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5 RELATED PATENT DOCUMENTS

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7 Closely related documents include coowned U. S. utility
8 patents and applications — all hereby incorporated by
9 reference in their entirety into this document. One is
10 U. S. 5,991,055 of Haselby et al., entitled "UNDERPULSED
11 SCANNER WITH VARIABLE SCAN SPEED, P. W. M. COLOR BALANCE,
12 SCAN MODES AND COLUMN REVERSAL" and of interest here for
13 its discussion of pulsed lamps of different colors, in
14 color sensing. Another such document is application se-
15 rial 08/960,766 of Bockman et al., entitled "CONSTRUCTING
16 DEVICE-STATE TABLES FOR INKJET PRINTING" and relevant for
17 its teaching of gray neutrality as a criterion for color
18 calibration at the gray axis and throughout the gamut —
19 and issued as U. S. Patent 6,____,____. A third related
20 document is application serial 09/183,819 of Baker, enti-
21 tled "COLOR-CALIBRATION SENSOR SYSTEM FOR INCREMENTAL
22 PRINTING", pertinent by virtue of its teaching of an aux-
23 illiary carriage and other variant components for use in
24 calibration — and issued as U. S. Patent 6,____,____.
25 Another somewhat related document is U. S. 5,657,137 of
26 Perumal, entitled "COLOR DIGITAL HALFTONING USING BLACK
27 AND SECONDARY COLOR REPLACEMENT", which takes up the proc-
28 esses of composite-black replacement and substitution.

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1 FIELD OF THE INVENTION

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3 This invention relates generally to devices and pro-
4 cedures for incremental printing of text or graphics on
5 printing media such as paper, transparency stock, or other
6 glossy media; and more particularly to a scanning thermal-
7 inkjet machine and method that construct text or images
8 from individual ink spots created on a printing medium, in
9 a pixel array. The invention is applicable to various
10 kinds of printing devices including facsimile machines and
11 copiers as well as printers.

12 Such "incremental" printing may be accomplished by
13 passing a single, full-page-width array (or one such array
14 for each of plural colorants) of marking elements continu-
15 ously along the length of a printing medium — or passing
16 the length of the medium under the array. Incremental
17 printing may instead be accomplished by passing a smaller
18 array (or again one for each of plural colorants) across
19 the width of the medium multiple times, in a process often
20 called "scanning" — the medium being advanced under the
21 scanning path or axis, between passes — to create a swath
22 or partial swath of marks in each pass.

23 In present-day commercial apparatus the grid is com-
24 monly a rectangular pattern of columns and rows, but for
25 purposes of this document need not be. For example a hex-
26 agonal pixel-grid pattern appears straightforwardly worka-
27 ble; and the invention would be applicable even in far
28 more remote grid forms, e. g. polar. The invention em-
29 ploys a colorant of a true black or secondary color as a
30 standard for correcting gray neutrality (absence of chro-
31 ma) or hue accuracy, respectively, of printing with three
32 or two superposed primary colorants.

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1 BACKGROUND OF THE INVENTION
23 (a) Color calibration and correction — Color cali-
4 bration is a known function in color printers. Its objec-
5 tive is to provide consistency of color within an image,
6 and among all images printed by a given printer, and from
7 printer to printer.8 Thus a proper color-calibration algorithm (CCA) com-
9 pensates for printer deviations in such a way that the
10 same nominal colorant values — i. e. quantities of cyan
11 (C), magenta (M), and yellow (Y) ink, and black (K) if
12 present — produce the same output from any printer which
13 undergoes the calibration. It is helpful to consider a
14 CCA as influencing 366, 368 (Fig. 15) a color-correction
15 stage 365, or the breakpoints 367 (i. e. the threshold
16 values) used in rendition, or both.17 Conventional color correction, sometimes referred to
18 as a "transfer function", is a one-dimensional mapping
19 (Fig. 16) for each colorant 381-84 respectively. In
20 eight-bit data processing for incremental-printing sys-
21 tems, ordinarily the color-correction mapping is from
22 eight bits of nominal colorant (C, M, or Y, or K if pres-
23 ent) to eight bits of printer-specific colorant.24 Various ways of forming a color-correction mapping
25 are known. In some products of the Hewlett Packard Compa-
26 ny, such mappings have been configured with the specific
27 aim of preserving the linearity of the colorants C, M and
28 Y — and again K if present.29 Experiments have shown, however, that linearity of
30 colorants, while providing an adequate solution for cer-
31 tain kinds of color variations such as those caused by
32 drop-weight fluctuation, nevertheless has distinct limi-
33 tations. These limitations are particularly troublesome
34 for inkjet printing. First, when primary colorants ex-

1 hibit a hue shift — such as often caused, with certain
2 media, by high humidity — the primary-linearity technique
3 helps only very little.

4 Second, this technique fails to ensure a critical
5 condition which is a hallmark of highest-quality printing
6 systems: gray neutrality, or in other words absence of
7 chroma, in nominally gray image features printed as combi-
8 nations of the primary chromatic colorants C, M and Y.

9
10 (b) Composite or process black and gray — It is
11 well known that combinations of these three subtractive
12 chromatic primaries produce a close approximation to
13 black, often called "process black". In the incremental-
14 printing industry, composite/process black or gray when
15 occurring outside highlight regions is usually replaced by
16 actual black ink when available.

17 The object of such replacement is to reduce both ink
18 usage and the volume of liquid deposited on the printing
19 medium — and also to circumvent possible problems due to
20 inaccuracy of the process-black approximation to actual
21 black. Not all incremental-printing devices, however,
22 have true-black ink cartridges. Therefore, in some such
23 devices, composite black is the only way to achieve any
24 black, and in such systems the accuracy of the process-
25 black approximation assumes greater importance.

26 In incremental printing an important use of process
27 black, or more precisely process gray, is for the benefit
28 of its mechanical capability to spread or distribute, over
29 a broader image area, colorant that appears neutral to the
30 eye (see the Perumal document mentioned earlier). In this
31 case the chromatic primaries are not overprinted but rath-
32 er are adjacent — or even scattered rather widely — so
33 that the overall impression of the visually integrated
34 dots is of a smoother or silkier texture, though still one

1 of a very light gray. Therefore, in this rather sophisticated
2 case, process gray is important even if actual black
3 ink is available.

4

5 (c) Inaccuracy — When used with less finesse, however,
6 process black — particularly in incremental printing — tends more toward being merely inaccurate. Discerning
7 observers detect some faint hue, some chromatic component, in image areas that are nominally gray.

8 This chromatic component arises from imperfectly balanced proportions of the three subtractive primary
9 colorants. The idea of "perfectly balanced proportions" unfortunately is ephemeral, because ideal proportions
10 actually vary with the chemical and colorimetric characteristics of the specific colorants employed.

11 Ideal proportions also vary with the electromechanical characteristics of the printheads used to apply the
12 colorants to the printing medium. All these factors typically vary from batch to batch of colorants and heads.

13 Furthermore these characteristics interact in confounding ways with characteristics of the printing medium,
14 and of the sequence and even the timing of colorant deposition — and these characteristics interact with each
15 other as well. The difficulty does not stop there, as ambient conditions including temperature and humidity also
16 interact with the foregoing factors to prevent any stable, single set of simple weight or volume proportions from
17 being usable over the life of a printing device.

18 The hue that appears in nominally gray regions, being uncontrolled, is most typically irrelevant to the subject
19 matter of the particular image features. Esthetically, therefore, it can often be quite jarring.

20

1 In perhaps more-technical terms, what is being per-
2 ceived is nonzero chroma. Colors that should be on the
3 central black-white axis of a theoretical perceptual color
4 space are instead reproduced slightly off-axis in one or
5 another direction within that space.

6 Such effects are least conspicuous in shadow and
7 highlight regions, where chroma is very difficult to de-
8 tect visually anyway. They are most obtrusive in midtone
9 regions, where chroma and hue are dominant characteristics
10 of human perception.

11 In incremental printing it is relatively rare for
12 artists to specify any particular inking effects for par-
13 ticular regions of an image. At least when using low-end
14 systems it is rather difficult even to gain access to con-
15 trols for such effects.

16 Instead the admixtures of physical colorants are sim-
17 ply left to the machine, without differentiation as to the
18 specific subject matter. Therefore most incremental
19 printing is particularly vulnerable to the adverse effects
20 of process black used unskillfully.

21

22 (d) Earlier correction of process-black chroma — It
23 is accordingly of particular importance that when process
24 black is used it be accurately black — that is to say
25 accurately neutral, nonchromatic. As noted above, howev-
26 er, the configuring of color-correction mappings to pre-
27 serve linearity in primary-colorant ramps fails to provide
28 this characteristic.

29 Some earlier products of the Hewlett Packard Company
30 use a color-correction mapping which is embodied in a cal-
31 ibration lookup table (see Bockman, mentioned above). The
32 table is formulated in the laboratory, most typically be-
33 fore a production line opens for a particular product. In
34 field operation, such a table is then read by a system

1 that is open-loop as to chroma — i. e., a system with no
2 feedback of field-measured gray-neutrality information to
3 the color-correction stage.

4 Other such products do print, measure and respond to
5 color test patterns in the field, but not with respect to
6 actual neutrality of nominally neutral patches made with
7 composite black/gray. More specifically, it is known to
8 canvass or assay generally throughout an entire device
9 gamut, approximating much of a color space. Although some
10 colors thus sampled and measured may be near the neutral
11 axis, this technique essentially approaches neutrality on
12 an incidental basis, and the actual neutrality of grays
13 achieved is correspondingly catch-as-catch-can.

14 It is also known — essentially as an opposite ex-
15 treme — to step through colorimetric measurement of in-
16 dividual-colorant ramps. This technique seeks to approach
17 the overall calibration as a matter of linearity of such
18 ramps, as suggested earlier. Without more, this method as
19 well yields inconsistent grays.

20

21 (e) Composite secondaries, and inaccuracy — Colors
22 that are well known as additive primaries in video work
23 (where all effects arise as colored lights) occur instead
24 as "secondaries" in printing (where all effects arise from
25 subtractive primary colorants). In printing therefore
26 red, green and blue are secondary colors, usually gener-
27 ated by adjacent or superposed yellow plus magenta, yellow
28 plus cyan, and cyan plus magenta, respectively.

29 The accuracy of each secondary accordingly depends
30 upon accuracy of the proportions of the subtractive prima-
31 ries used. For instance the accuracy of red, formed from
32 yellow and magenta, depends upon the accuracy of propor-
33 tions of the yellow and magenta colorants used.

1 Here too, as in the foregoing process-black discus-
2 sion, the definition of "accuracy of proportions" is a
3 very elusive concept because optimum proportions really
4 depend upon a complex of attributes, including those of
5 the colorants, colorant-application devices, printing
6 medium, deposition sequence and timing, temperature and
7 humidity. Nevertheless, just as there is a clear defini-
8 tion of what is meant by "gray neutrality", it is possible
9 to fashion clear (if spectrally complicated) definitions
10 of what is meant by "red", "green" and "blue".

11 When these colors are not produced accurately, the
12 resulting esthetic impression can be even more troublesome
13 than slight chroma within regions that are nominally gray.
14 This is so for two reasons.

15 First, only limited sorts of objects in color photos
16 depend for their realism upon total absence of chroma.
17 Second, inaccuracies in the color secondaries manifest
18 themselves as hue shifts, to which observers typically re-
19 spond by saying that the colors are "off".

20 Results can be especially conspicuous in flesh tones
21 that have a strikingly unnatural cast, or in other objects
22 of well-known but inaccurately rendered hue that observers
23 may describe as "wrong". Earlier efforts to deal with the
24 problem of inaccurate secondaries have suffered either
25 from complete absence of secondary-accuracy feedback
26 information or — in systems that rely on field spectral
27 measurements using wideband sensing — at least from
28 absence of reliable hue references for those colors.

29
30 (f) Conclusion — Chroma appearing in nominally gray
31 regions, and secondary-color hue errors, have continued to
32 impede achievement of uniformly excellent inkjet printing.
33 Thus important aspects of the technology used in the field
34 of the invention remain amenable to useful refinement.

1

2

3 SUMMARY OF THE DISCLOSURE

4

5 The present invention introduces such refinement.
6 Before presenting a relatively formal introduction of the
7 invention, it may be helpful to mention some insights that
8 are considered part of the inventive process.

9 The process-black miscalibration problem discussed
10 above arises precisely from the previously mentioned in-
11 dependence of the prior-art mappings for the different
12 colorants. In such mapping regimes there is no place to
13 introduce crosscomparisons, and associated adjustments —
14 to remove the subtle intrusions of residual chroma which
15 can become so conspicuous in particular midtone features.

16 Similarly as to secondary colors that appear "off" or
17 "wrong", conventional mapping schemes rely on wideband
18 sensing. Such measurements can go awry because of various
19 different effects.

20 One class of errors arises from metameric effects.
21 For instance, these types of measurement may implicitly
22 assume that the colorant has a particular spectral-reflec-
23 tance curve — which may in fact be very different from
24 that of the colorants being used. The sensor system in
25 the printing device integrates the reflected colors dif-
26 ferently than does the human visual mechanism.

27 It will be understood that the invention as practiced
28 and as defined in the appended claims does not rely for
29 its validity or utility upon correctness of these com-
30 ments. Now with these observations in mind, this discus-
31 sion will turn to a somewhat more-rigorous presentation.
32

33 In its preferred embodiments, the present invention
34 has several aspects or facets that can be used independ-

1 ently, although they are preferably employed together to
2 optimize their benefits.

3 In preferred embodiments of a first of its facets or
4 aspects, the invention is a method for color-calibrating a
5 printing device. The method includes the steps of using
6 the printing device to print a gray ramp with black ink,
7 and using the same printing device to print a nominally
8 gray ramp with composite-black ink.

9 In addition the method includes the step of measuring
10 and comparing the printed gray ramps. A further step is
11 employing the measured black-ink ramp as a standard to
12 correct the measured composite-black ramp.

13

14 The foregoing may represent a description or defini-
15 tion of the first aspect or facet of the invention in its
16 broadest or most general form. Even as couched in these
17 broad terms, however, it can be seen that this facet of
18 the invention importantly advances the art.

19 In particular, this method enables a printing system
20 to find the needed actually neutral combination not only
21 very precisely but also with relatively high assurance of
22 accuracy. This is because the system will closely match
23 the composite coloration to the actual black-ink values,
24 which are essentially unquestioned. The system carries
25 its neutral standard along with it, in actual physical
26 form.

27

28 Although the first major aspect of the invention thus
29 significantly advances the art, nevertheless to optimize
30 enjoyment of its benefits preferably the invention is
31 practiced in conjunction with certain additional features
32 or characteristics. In particular, preferably all the
33 steps are performed automatically.

1 Also preferably the employing step includes treating
2 the black-ink ramp as a zero-chroma standard to correct
3 chroma found in the composite-black ramp. A third pref-
4 erence is using the compared black-ink and composite-black
5 ramps to also correct other printing with composite black.

6 In this latter case there is a subpreference. It is
7 that the method further use the compared black-ink and
8 composite-black ramps to also correct other colors to be
9 printed by the printer.

10 Yet another basic preference is that the using step
11 with composite-black ink include printing, for a particu-
12 lar gray tonal level, plural combinations of nonblack
13 inks; and in this case it is still further preferable that
14 the plural combinations of nonblack inks substantially
15 bracket nominal values for the particular gray value.

16 To this last-mentioned preference there are two sep-
17 arate subpreferences, namely that the employing step (or
18 the measuring and comparing step) include searching the
19 printed and measured plural combinations of nonblack inks
20 to find, respectively:

21

- 22 ■ a combination that is nearest the corresponding
23 particular gray value; or instead

24

- 25 ■ at least two combinations that bracket a correspond-
26 ing particular gray value — and then interpolating
27 among the at least two combinations to determine an
28 optimal combination for matching the corresponding
29 particular gray value.

30

31 In the case of this second subpreference, the bracketing
32 is preferably optimized. Optimized bracketing in turn
33 preferably includes printing with the plural combinations
34 of nonblack inks that surround the nominal value in a

1 pattern, in color space, that is substantially centered on
2 the nominal value.

3 Now reverting to the above-mentioned basic preference
4 of printing plural combinations of nonblack inks for a
5 particular gray tonal level, another subpreference is that
6 the employing (or the measuring and comparing) step
7 include searching the printed and measured plural combi-
8 nations of nonblack inks to find a combination that is
9 nearest a corresponding particular gray value.

10
11 Yet another basic preference is that the measuring
12 and comparing step (and/or the employing step) include
13 inserting measured values of the printed gray ramps into
14 equations representing a colorimetric model of the prin-
15 ter, and solving the equations to derive correction values
16 for use in adjusting ink signals in future printing. A
17 subpreference is that the colorimetric equations be solved
18 by iteration.

19 A particularly preferred form of these colorimetric
20 equations includes plural multiplicative expressions:

21
22 $H(t, n, a) = D(t, n) \cdot E(t, n) \cdot \dots \cdot F(t, n)$, [1]

23
24 wherein H is a composite or hybrid color printed by use of
25 at least two constituent colors,
26 D is one of the constituent colors,
27 E is another of the constituent colors,
28 ". . ." represents possible additional constituent
29 colors of the at least two,
30 F is a correction factor,
31 t is a tonal level at which H , D , E and ". . ."
32 are evaluated,
33 n is a sensor channel at which all the above are
34 evaluated, and

1 a is a scaling factor that relates overall range
2 of the hybrid color with overall range of the
3 constituent colors.

4

5 When these equations are used, preferably in some of
6 the expressions, $H = cK$, $D = S_1$ and $E = S_2$, where cK is
7 composite black and S_1 and S_2 are secondaries; and in
8 others of the expressions, $H = S$, $D = P_1$ and $E = P_2$, where
9 S is a secondary and P_1 and P_2 are primaries. In this
10 case, still further preferably, in the others of the ex-
11 pressions a = 1.

12 Although the equations in multiplicative form are
13 particularly preferred, another favored general form is
14 instead additive, for example —

15

$$16 \quad H(t, n, a) = D(t, n) + E(t, n) \cdot F(t, n) \\ 17 \quad \quad \quad \quad \quad \quad + E'(t, n) \cdot F'(t, n) + \dots \quad [2]$$

18

19

20 In preferred embodiments of its second major indepen-
21 dent facet or aspect, the invention is a self-calibrating
22 color printer. The printer includes some means for print-
23 ing a nominally gray ramp using composite black. For
24 purposes of generality and breadth in discussing the in-
25 vention, these means may be called the "composite-black
26 using means" or simply the "using means".

27 The printer also includes some means for measuring
28 the printed ramp in at least two different spectral bands
29 respectively. Again for breadth and generality these
30 means will be called the "measuring means".

31 In addition the printer includes a programmed proces-
32 sor for modifying subsequent operation of the printer to
33 substantially compensate for any nonzero chroma in the
34 printed nominally gray ramp. As will be understood, the

1 programmed processor for performing this function may take
2 the form of portions of one or more processors that manage
3 the whole operation of the entire printer.

4

5 The foregoing may represent a description or defini-
6 tion of the second aspect or facet of the invention in its
7 broadest or most general form. Even as couched in these
8 broad terms, however, it can be seen that this facet of
9 the invention importantly advances the art.

10 In particular, this document earlier points out that,
11 on the one hand, colorimetric measurement of individual-
12 colorant ramps is known; and that on the other hand col-
13 orimetric measurement aiming to assay generally over an
14 entire color-space or gamut is known. A composite-black
15 ramp as such serves much better to probe and establish
16 actual gray neutrality than either of those diametrical
17 prior techniques.

18 Furthermore, specifically testing the nominally neu-
19 tral ramp for chroma — i. e. for neutrality as such —
20 not only far more effectively develops information for
21 achieving grays that are substantially free of chromatic
22 cast. In addition these grays in turn form a sturdy and
23 reliable central-axis chromatic backbone for accurate
24 color surrounding that axis.

25

26 Although the second major aspect of the invention
27 thus significantly advances the art, nevertheless to
28 optimize enjoyment of its benefits preferably the inven-
29 tion is practiced in conjunction with certain additional
30 features or characteristics. In particular, preferably
31 the measuring means include means for measuring the prin-
32 ted ramp in at least three different spectral bands.
33 While something can be accomplished using two, and it is

1 believed novel and unobvious to do so, results with three
2 bands are very superior.

3 It is also preferable that the measuring means in-
4 clude at least two different lamps for illuminating the
5 printed ramp, and at least one sensor for detecting lamp
6 illumination reflected from the printed ramp. In this
7 case it is further preferable that those lamps be light-
8 emitting diodes, emitting different colors respectively.

9 Another basic preference — in essence alternative to
10 the one just described — is that the measuring means in-
11 clude means for illuminating the printed ramp in at least
12 two spectral bands, and at least one sensor for detecting
13 illumination reflected from the printed ramp in those
14 spectral bands separately. In this case it is further
15 preferable that the illuminating means include a lamp
16 emitting in the two or more spectral bands; and that the
17 sensor include spatially, temporally or absorptively
18 selective means for separating illumination from the at
19 least two spectral bands.

20 An additional basic preference is that the programmed
21 processor include compensation means for adjusting subse-
22 quent operation to substantially minimize chroma in print-
23 ing of nominal gray. In this case a further preference is
24 that the compensation means include means for reducing
25 chroma, in printing of nominal gray, to ΔE of approximate-
26 ly 2.5 or less. The notation " ΔE " represents the color
27 distance in the CIEL*a*b* space.

28

29

30 In preferred embodiments of its third major independ-
31 ent facet or aspect, the invention is a method for auto-
32 matically color-calibrating a printer. The method includes

1 the step of using the printer to print a ramp in a partic-
2 ular color with actual ink of that color.

3 In addition the method includes using the same prin-
4 ter to print a ramp nominally in the particular color but
5 with inks of other colors; and then measuring and compar-
6 ing the printed ramps. Yet another step is using the
7 measured actual-ink ramp as a standard to calibrate and
8 correct the measured other-colors-ink ramp — and also to
9 correct other printing with those other colors.

10

11 The foregoing may represent a description or defini-
12 tion of the third aspect or facet of the invention in its
13 broadest or most general form. Even as couched in these
14 broad terms, however, it can be seen that this facet of
15 the invention importantly advances the art.

16 In particular, this aspect of the invention more
17 broadly provides benefits analogous to those discussed
18 above for the first aspect. These benefits are provided
19 now with respect to precision, accuracy and reliability of
20 composite secondaries, as well as composite black.

21

22 Although the third major aspect of the invention thus
23 significantly advances the art, nevertheless to optimize
24 enjoyment of its benefits preferably the invention is
25 practiced in conjunction with certain additional features
26 or characteristics. In particular, preferably the actual
27 ink is red ink, green ink, or blue ink — and the inks of
28 other colors are magenta ink and yellow ink in combina-
29 tion, or yellow ink and cyan ink in combination, or cyan
30 ink and magenta ink in combination.

31

32 In preferred embodiments of its fourth major indepen-
33 dent facet or aspect, the invention is a method for auto-
34 matically color-calibrating a printer. The method compri-

1 ses the steps of modeling an actual color-reproduction
2 system of the printer in a color space that is transformed
3 by contraction.

4 The contraction brings the machine-primary color axes
5 closer to neutral gray. Another step of the method is
6 performing a color calibration in the contracted model of
7 the printer color-reproduction system.

8 Still another step of the method is applying a re-
9 verse transform to reexpand the calibration results. That
10 is, the calibration is expressed in terms of the actual
11 color-reproduction system of the printer.

12
13 The foregoing may represent a description or defin-
14 ition of the fourth aspect or facet of the invention in
15 its broadest or most general form. Even as couched in
16 these broad terms, however, it can be seen that this facet
17 of the invention importantly advances the art.

18 In particular, by operating in a contracted machine
19 space this facet of the invention enables the calibration
20 procedure to operate much more finely. This method there-
21 by yields a more precise and generally more accurate over-
22 all result.

23 Although the fourth major aspect of the invention
24 thus significantly advances the art, nevertheless to
25 optimize enjoyment of its benefits preferably the inven-
26 tion is practiced in conjunction with certain additional
27 features or characteristics. In particular, preferably
28 this facet of the invention is practiced in conjunction
29 with the first three, introduced above.

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33 All of the foregoing operational principles and
34 advantages of the present invention will be more fully

1 appreciated upon consideration of the following detailed
2 description, with reference to the appended drawings, of
3 which:

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7 BRIEF DESCRIPTION OF THE DRAWINGS

8
9 Fig. 1 is a partly diagrammatic showing of color pat-
10 ches for calibrating a single tonal level in a composite-
11 black neutral ramp, by comparison with a true-black ramp;

12 Fig. 2 is a graph of representative sensor responses
13 in three channels, for both composite and true black, at a
14 common nominal tonal level — for preliminary determina-
15 tion of needed rescaling;

16 Fig. 3 is a conceptual graph showing representative
17 spectral sensitivities in the three sensor channels;

18 Fig. 4 is a test pattern with primary ramps (in the
19 top row) of cyan, magenta, yellow and black — followed by
20 composite ramps, in the bottom row, of red (yellow plus
21 magenta), green (cyan plus yellow), blue (magenta plus
22 cyan) and black (all three primaries);

23 Fig. 5 is a conceptual graph showing how the three
24 primary colorants influence (ideally) the three sensor
25 channels;

26 Fig. 6 is a like graph but showing how the behavior
27 of each primary in a nominally black composite printout is
28 adjusted, according to the invention, to make the compos-
29 ite actually match true black;

30 Fig. 7 is a graph of reflectivity as a function of
31 wavelength for each primary and the bare printing medium;

32 Fig. 8 is a numerical example, in the form of a tabu-
33 lation, showing how the Fig. 2 rescaling is completed;

1 Fig. 9 is a graph of the above-introduced contraction
2 principle of the invention, diagrammed in CMY space, with
3 the solid and dashed colored lines C, M, Y, C', M' and Y'
4 being the original and modified axes respectively — thus
5 showing how the axes are shrunk, in terms of the angle of
6 deviation;

7 Fig. 10 is a perspective drawing of the invention as
8 incorporated into a representative printing device that is
9 a large-format printer/plotter;

10 Fig. 11 is a like drawing of the scanning subsystem
11 which carries printheads and a sensor across the printing
12 medium in the Fig. 10 device;

13 Fig. 12 is a block-diagrammatic representation of a
14 hardware system, incorporating the Fig. 10 and 11 prin-
15 ter/plotter, according to the invention;

16 Fig. 13 is a partial view with an alternative sensor;

17 Fig. 14 is a flow chart for a method according to the
18 invention;

19 Fig. 15 is a high-level flow chart indicating the re-
20 lationship between a color-calibration algorithm (CCA), a
21 color-correction stage and a rendition stage; and

22 Fig. 16 is an exemplary color-correction mapping.

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24

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26 DETAILED DESCRIPTION

27 OF THE PREFERRED EMBODIMENTS

28

29 1. GRAY NEUTRALITY AS A COLOR-CORRECTION STANDARD

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31 Experiments have shown that building the transfer
32 functions in such a way as to establish gray neutrality
33 foremost, instead of individual-primary linearity, yields
34 better results. In particular, remarkably, the previously

1 mentioned extreme sensitivity of colors to humidity is
2 greatly reduced.

3 Furthermore, as mentioned earlier, gray neutrality is
4 itself a desired property of the printer. With this tech-
5 nique this property is ensured.

6 The gray-neutrality approach, like some prior meth-
7 ods, is reliant upon comparative measurements of just-
8 printed test patterns — using a sensor 251 (Figs. 11
9 through 13). As a matter of convenience, in printing
10 devices of the scanning type the sensor is most typically
11 mounted on the carriage 220 which holds the printheads.

12 This arrangement enables positioning of the sensor
13 automatically over any part of the test pattern (Fig. 1 or
14 4) on the printing medium 4A (Figs. 12, 13). It is a par-
15 ticularly advantageous arrangement in that many printing
16 devices already carry a so-called "line sensor" on the
17 carriage, for use in alignment, edge tracking and so on.

18 Thus use of the already-available line sensor makes
19 double duty of that component, achieving additional func-
20 tionality at substantially no cost. The line sensor, how-
21 ever, is not necessarily an ideal choice: it is designed
22 for simple geometrical measurements and not optimized for
23 colorimetry.

24 The previously mentioned Baker document teaches al-
25 ternatives such as use of an auxiliary carriage with a
26 sensor of finer quality. Depending on the importance of
27 colorimetric accuracy in a particular printing device, the
28 line sensor may be entirely adequate.

29 In operation, a true-black ramp e. g. 174 (also seen
30 as individual patches 101) is measured and compared with
31 approximations using composite black 179 (also 111, 121-
32 25, 131-35). The composite-black approximation is then
33 very delicately refined to approach the true-black ramp
34 very precisely.

1 This refinement, maintained (in effect, propagated)
2 throughout the gamut of the printing device, constitutes
3 the desired calibration for use in all subsequent printing
4 until the next calibration. Two alternative ways of cali-
5 brating, both based on this principle, are described in
6 the two subsections that follow.

7 For purposes of this document, preferably a three-
8 lamp (typically three-LED) sensor 251, 251' (Fig. 12) is
9 in use, but as detailed below a single broadband lamp
10 251'BB (Fig. 13) may be substituted as preferred. Before
11 the calibration procedure itself is started, the true-
12 black ramp should be linearized using conventional linea-
13 rization techniques or better.

14
15
16 2. COMPLETE SAMPLING

17
18 (a) General procedure — This may be regarded as the
19 most straightforward method for performing the gray-neu-
20 trality calibration:

21
22 ■ A black patch 101 (Fig. 1) is printed and measured,
23 for a particular tonal level (in the illustrated
24 example, fifty percent).

25
26 ■ A sampling 111, 121-125, 131-135 of the composite
27 black nominally near the same level, including small
28 variations 121-125, 131-135 in all colorant dimen-
29 sions (C, M, Y), is printed and measured.

30
31 ■ The most similar composite-black patch e.g. 123 is
32 chosen as the corrected value.

1 The number of patches to be printed is at least $3^3 = 27$,
2 corresponding to at least three colorants (C, M, Y) and at
3 least three states (+, =, - or in words "high", "nominal"
4 and "low").

5 The sampling can be grosser or finer, and some simple
6 interpolation (e. g. linear or cubic) can be performed to
7 improve the accuracy. Thus more than three states may be
8 sampled (for instance ++, +, =, - and --).

9 The printing system may have more than three chromat-
10 ic colorants, as for example including dilute magenta and
11 dilute cyan. If so, it is advisable to include the addi-
12 tional colorants in the calibration procedure.

13 The same procedure is repeated for as many points as
14 desired (usually between eight and sixteen), along the
15 gray gamut from black nearly to white. In this way the
16 full gray-scale range is adjusted. Next the transfer
17 functions are calculated based on these correction values.
18

19 (b) Range — The black and composite-black ranges
20 may not be, and usually are not, the same. Most commonly
21 the true-black gamut extends further toward the dark end
22 of the gray axis than does composite black.

23 To resolve this range misfit, the system does not at-
24 tempt to match equal densities, e. g. fifty percent com-
25 posite black with fifty percent true black. Instead a
26 rescaling is performed — to match one hundred percent of
27 composite black against e. g. eighty percent of true
28 black.

29 (c) Centerpoint, sampling shape and sequencing — It
30 is very likely that the correct combination of C, M and Y
31 that yields gray is quite far from equal amounts of those
32 primaries. Therefore it may be very inefficient to per-
33 forming sampling that is centered on equal amounts.

1 To improve efficiency, and in some cases accuracy as
2 well, the tendency of the prior points (for instance, they
3 may all be ten percent and higher for one primary) may be
4 extrapolated. For example, if there is always a need for
5 slightly more magenta, the sampling may be centered at +5%
6 magenta at the outset.

7 Further, the sampling in CMY space need not be cubi-
8 cal, i. e. $\pm/=\pm$ for each of the three inks. It can also
9 be a sphere, a pyramid, or any other geometrical arrange-
10 ment that provides a reasonable sampling of the colorant
11 space around or near the nominal combination of values.

12 If desired the search for best neutral match can be
13 further refined by iteration, with different increments of
14 sampling. At each pass, the solutions are used as new
15 centerpoints.

16 In other words, a first pass may be performed with
17 $\pm 10\%$ variation about zero (or about e. g. +5% magenta as
18 suggested above), yielding a best solution. A new pass is
19 then performed with $\pm 5\%$ variation about that best solution — and
20 so on for some specified number of iterations or until the
21 solution converges to some specified precision.

23

24 (d) Advantages: robustness, minimum storage — In
25 addition to the benefits of the gray-neutrality on its
26 own, the algorithms discussed here are particularly resis-
27 tant to LED variations. This is due to the fact that the
28 interpretation of all measurements is relative rather than
29 absolute.

30 Because all the corrections are based upon relative
31 rather than absolute quantities, practice of the invention
32 requires no LED characterization table or the like. The
33 only constraint is that the illumination be approximately
34 a partition of the visible spectrum.

1

2 3. MODELING

3

4 Modeling is in essence a tactic for reducing the num-
5 ber of patches to be measured, by invoking some accurate
6 process of estimation. This tactic reduces the time re-
7 quired for printing and measuring, along with the quanti-
8 ties of printing medium and colorant required.

9 Many models are possible. The general technique of
10 modeling for other predictive or corrective purposes, how-
11 ever, is known; hence people skilled in this field will
12 find the simple examples discussed here adequate to guide
13 practice of the present invention.

14

15 (a) Measurement — If a three-LED sensor (e. g. line
16 sensor) — or broadband illumination with three-band spec-
17 tral differentiation — is used, the sensing system can be
18 regarded as a three-broadband spectral detector with three
19 main channels: red 146 (Fig. 3), green 147 and blue 148.
20 In preferred embodiment of the invention, this detector
21 measures reflected light from a test pattern made up of
22 pure-colorant ramps 171-174 (Fig. 4) and composite ramps
23 176-179.

24 The pure-colorant part of the pattern includes one
25 ramp each for cyan 171, magenta 172, yellow 173 and black
26 174. The composite part includes one ramp each for red (a
27 magenta-plus-yellow composite) 176, green (cyan plus yel-
28 low) 177, blue (cyan plus magenta) 178 and black (cyan
29 plus magenta plus yellow) 179.

30 With each sensor channel in turn — i. e., with each
31 LED — the system measures the chromatic primaries (CMY),
32 the secondaries (R=M+Y, G=Y+C, B=C+M), the composite-black
33 (cK=C+M+Y) and the black (K) ramps. It is a matter of op-
34 erational convenience and design choice whether the entire

1 pattern is measured with each sensor channel before moving
2 on to the next sensor channel, or instead the measurements
3 in all three channels are performed in each part of the
4 pattern before proceeding to the next part of the pattern.

5 The latter approach, however, is generally preferable
6 as a practical matter, since flashing LEDs through a cycle
7 (see Haselby) can be accomplished very quickly — requir-
8 ing no mechanical movement of the printhead carriage or
9 printing-medium advance drive. If desired, such measure-
10 ments can be made while the mechanical systems are in mo-
11 tion (incurring an accuracy penalty due to measuring dif-
12 ferent portions of each patch, in the different spectral
13 bands). Hence cycling through the LEDs, at each patch, in
14 principle can provide an entire measurement-data array
15 with just one slow pass over each row of the test pattern.
16

17 (b) Meaning of the data — In each printer the re-
18 sults of the ramp measurements will be a family of numeri-
19 cal tabulations, i. e. data arrays —

20
21 $C = C(t, n)$
22 $M = M(t, n)$ [3]
23 $Y = Y(t, n)$

24
25 in which t is the nominal tonal value, along the ramp, for
26 which each measurement is made (often expressed as a col-
27 orant percentage or fraction), and n the sensor channel
28 (r, g, b) used to make the measurement.

29 At the outset, these data represent simply the numer-
30 ical value of reflectance uniquely corresponding to each
31 specified combination of ramp position and channel. That
32 is to say, at this stage the t and n values are the inde-
33 pendent variables, and the C, M, Y values, the dependent.

34

1 It is helpful, however, to look ahead to the end of
2 the process and keep in mind that the values of t — when
3 later divorced from channel indices n = r, g, b and also
4 when referred to the primary colorants CMY of the printing
5 system rather than the sensor channels r, g, b — will be-
6 come the dependent variables that will be sought as the
7 end result of the calibration process. In particular
8 these numbers t are the tonal values which the printing
9 stage must be instructed to produce, to obtain particular
10 tonal values of gray:

$$\begin{aligned}
 11 & & & \\
 12 & \underline{t}_c = \underline{t}(\underline{t}_k) & & \\
 13 & \underline{t}_M = \underline{t}(\underline{t}_k) & [4] & \\
 14 & \underline{t}_Y = \underline{t}(\underline{t}_k) . & &
 \end{aligned}$$

16 In general this correspondence will not be an equal-
17 ity. In other words when a particular tonal value t_K of
18 gray is desired, the printing device must in general be
19 directed to produce some other tonal values t_C , t_M , t_Y of
20 C, M and Y respectively —

22	$\underline{t}_c \neq \underline{t}_k$	
23	$\underline{t}_m \neq \underline{t}_k$	[5]
24	$\underline{t}_x \neq \underline{t}_k$	

26 and this inequality in fact is why calibration is needed.

Now with the perspective in mind that the tonal-value numbers t will be the variables sought, it can be correspondingly appreciated that the photometric-measurement numbers C, M, Y —

32 $C = C(\underline{t}, \underline{n})$
33 $M = M(\underline{t}, \underline{n})$ [6]
34 $Y = Y(\underline{t}, \underline{n})$

1 will later be the data to be read from the tabulations, in
2 the final steps of solving for t_c , t_M , t_Y . The usefulness
3 of the initial data tabulation resides in the fact that
4 the uniqueness of the tabulation works in both directions.

5 Thus the measured C, M, Y values can be simply read
6 out from the tabulation in response to desired values of
7 t_c , t_M , t_Y . Moreover, intermediate values of the nominal
8 C, M, Y data are available through interpolation. Accord-
9 ingly each needed value of C, M or Y for a particular col-
10 or will be inferred directly, through the tabulation, by a
11 corresponding specified value of t .

12
13 (c) Nonideal behavior of colorants — Interpretation
14 of the sensor data proceeds by construing the common re-
15 sponse 151 (Fig. 5) in the red and green channels r , g as
16 representing cyan. Similarly, the common response 152,
17 153 in the red and blue channels r , b is construed as rep-
18 resenting magenta, and the common sensor response 154 in
19 the green and blue channels g , b as representing yellow.
20 Imperfections in these assumptions are discussed below.

21 The invention seeks to determine which amount of each
22 colorant is needed to achieve a neutral composite black
23 (cK). If inks actually behaved ideally in the sense that
24 coloring effects were confined to respective nonoverlap-
25 ping sensor channels — as described in the preceding
26 paragraph — then measuring only the primaries (CMY) and
27 black (K) would suffice.

28 In that case, the response 156, 157, 158 (Fig. 6) of
29 each primary (CMY) would simply be adjusted to produce the
30 same response 141 as the black colorant. Unfortunately
31 inks do not behave in that way — as seen from the fact
32 that the primary response curves 161-164 (Fig. 7) are not
33 rectangular functions at all but rather continuous curves

1 with quite different behavior in different spectral regions.

2 For instance the cyan reflectivity 161 is not equal
3 in the blue and green as suggested 151 in Fig. 5, but in-
4 stead peaks in the blue and falls with increasing wave-
5 length through the green. It even displays minor return
6 161' in the far red.

7 Analogously the magenta reflectivity 162, 163 is not
8 equal in the blue and red as suggested 152, 153 in Fig. 5.
9 Instead it has by far its major return 162 in the red and
10 only a relatively quite small subsidiary return 162 in the
11 blue.

12 Still further, yellow reflectivity 164 is not equal
13 in the green and red as suggested 154 in Fig. 5, but in-
14 stead falls off in the lower end of the green band. It
15 returns quite significantly into the blue, where in ideal
16 terms it should be substantially nonreflective.

17 Not even the reflectivity 166 of the printing medium
18 is wholly as might be classically expected, since its
19 reflectivity falls abruptly in the lower end of the blue.
20 To complicate matters still further the reflectivity of
21 pure, true black ink is anomalously very substantial in
22 the far red — exceeding, for instance, that of the magen-
23 ta peak 162 in the blue.

24

25 (d) Model equations — To compensate these cross-
26 channel and other nonideal effects, we build a model to
27 describe actual ink behavior. At the outset a general
28 multiplicative expression may be noted, for use in rela-
29 tion to both secondary colorants and black (repeating
30 equation [1]):

31

32 $H(\underline{t}, \underline{n}, \underline{a}) = D(\underline{t}, \underline{n}) \cdot E(\underline{t}, \underline{n}) \cdot \dots \cdot F(\underline{t}, \underline{n})$. [1']

33

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1 Here H is a hybrid or composite color printed by use of at
2 least two constituent colors,

3

4 D is one of the constituent colors,
5 E is another of the constituent colors,
6 ". . ." represents possible further constituent
7 colors of the "at least two",
8 F is a correction factor,
9 \underline{t} is a tonal level at which H, D, E and ". . ."
10 are evaluated,
11 \underline{n} is a sensor channel at which all the above are
12 evaluated, and
13 \underline{a} is a scaling factor that relates overall range
14 of the hybrid color with overall range of the
15 constituent colors.

16

17 In some of the expressions, H = cK, D = S_1 and E =
18 S_2 , where cK is composite black and S_1 and S_2 are secondaries.
19 In others of the expressions, H = S, D = P_1 and E =
20 P_2 , where S is a secondary and P_1 and P_2 are primaries; in
21 these latter expressions, $\underline{a} = 1$.

22 Now to demonstrate application of this general ex-
23 pression to the several cases involved in accordance with
24 the invention, consider first forming the secondaries —
25 with the correction factor $F(\underline{n}) = \alpha_{\underline{n}}$:

26

$$\begin{aligned} 27 \quad R(\underline{t}, \underline{r}) &= M(\underline{t}, \underline{r}) \cdot Y(\underline{t}, \underline{r}) \cdot \alpha_R(\underline{t}) \\ 28 \quad G(\underline{t}, \underline{g}) &= C(\underline{t}, \underline{g}) \cdot Y(\underline{t}, \underline{g}) \cdot \alpha_G(\underline{t}) \quad [7] \\ 29 \quad B(\underline{t}, \underline{b}) &= C(\underline{t}, \underline{b}) \cdot M(\underline{t}, \underline{b}) \cdot \alpha_B(\underline{t}), \end{aligned}$$

30

31 where

32 R, G and B are the colors being formed as ink
33 combinations,

1 M, Y and C are the constituent colors,
 2 α is the correction factor,
 3 t is a tonal level (equivalently, an ink percen-
 4 tage) at which M, Y, C and α are evaluated, and
 5 r , g and b are the sensor channels at which all
 6 the above are evaluated.

7

8 For example $C(0.7, g)$ means the sensor reading in the green
 9 channel on a nominally 70% patch of cyan.

10 Preliminary to finding a solution to the overall mod-
 11 eled system — as will be shown below — the foregoing
 12 three expressions are rearranged to solve for the three
 13 correction factors α :

$$\begin{aligned} \alpha_r(t) &= \frac{R(t, r)}{M(t, r) \cdot Y(t, r)} & [8] \\ \alpha_g(t) &= \frac{G(t, g)}{C(t, g) \cdot Y(t, g)} \\ \alpha_b(t) &= \frac{B(t, b)}{C(t, b) \cdot M(t, b)} . \end{aligned}$$

21 Thus a numerical value for the correction factor $\alpha_g(0.7)$
 22 is obtained from the three sensor measurements $G(0.7, g)$,
 23 $C(0.7, g)$ and $Y(0.7, g)$.

24 In some situations there is a small complication con-
 25 cerning the tonal values (or color percentage) to which
 26 the correction factors α apply. In the determination of
 27 those factors, only one tonal value is involved — because
 28 the same tonal value is specified for both e. g. magenta
 29 and yellow in forming red; and that same tonal value is
 30 attributed to the resulting red patch as well.

31 In a more-advanced model, however, as will be seen,
 32 it can be preferable to estimate red from different per-
 33 centages of magenta and yellow — and analogously for the

1 other secondaries. In order to simplify the model, none-
2 theless, each correction factor α is computed unidimension-
3 nally, and its index is the average of the tonal values of
4 its two constituents:

5
$$\alpha(t_M, t_Y) = \alpha\left(\frac{t_M + t_Y}{2}\right) . \quad [8]$$

8 A more complex model would yield better results but
9 would require more samples. To simplify the notation, in
10 most of the remainder of this discussion when referring to
11 the correction factors α no sensor channel will be speci-
12 fied for the tonal values. That is, for example correc-
13 tion factors $\alpha_G(0.7)$, $\alpha_R(0.3)$ and $\alpha_B(0.9)$ will all be
14 written simply $\alpha(0.7)$, $\alpha(0.3)$ and $\alpha(0.9)$ respectively.

16 The foregoing discussion explores application of a
17 general expression for a composite color H to composite
18 secondary colors. Next consider application of the same
19 general expression to composite grays:

21
$$cK(t, r) = C(t, r) \cdot R(t, r) \cdot \beta_R(t)$$

22
$$cK(t, g) = M(t, g) \cdot G(t, g) \cdot \beta_G(t) \quad [9]$$

23
$$cK(t, b) = Y(t, b) \cdot B(t, b) \cdot \beta_B(t) ,$$

25 where

26 cK is composite black, formed as a three-colorant
27 combination of cyan, magenta and yellow (CMY),
28 C , M and Y are those constituent primary colors,
29 R , G and B are red, green and blue as two-colorant
30 combinations of those primaries,
31 β is a correction factor in each channel
32 respectively,

1 \underline{t} is a tonal level (equivalently, an ink percen-
 2 tage) at which C, M, Y and β are evaluated, and
 3 r , g and b are the sensor channels at which all
 4 the above are evaluated.

5

6 Analogously to the preliminary step in the primary-
 7 colorant case discussed earlier, the foregoing three ex-
 8 pressions are rearranged to solve for the three correction
 9 factors β :

$$10 \quad \beta_r(t) = \frac{cK(t, r)}{C(t, r) \cdot R(t, r)} \quad [10]$$

$$11 \quad \beta_g(t) = \frac{cK(t, g)}{M(t, g) \cdot G(t, g)}$$

$$12 \quad \beta_b(t) = \frac{cK(t, b)}{Y(t, b) \cdot B(t, b)} \quad .$$

13 Here as with the α derivations discussed earlier, actual
 14 numerical values can now be obtained for β , to be inserted
 15 into final expressions for \underline{t} . Here, to avoid circular
 16 definition in each channel, the same tone-definition issue
 17 discussed above for α calculations recurs; for example:

$$18 \quad \beta_g(t_m, t_g) = \beta_g\left(\frac{t_m + t_g}{2}\right) = \beta_g\left(\frac{t_m + \frac{t_c + t_y}{2}}{2}\right) \quad [11]$$

19 (e) Condition — Solution of the system of equations
 20 requires one further constraint. The constraint to be im-
 21 posed is simply that composite black cK matches true black
 22 K at all bands, or more precisely all bands that can be
 23 measured — in other words, in all the sensor channels.

24 In the notation introduced above, this condition ap-
 25 pears thus:

1 $cK(\underline{t}, \underline{r}) = K(\underline{a}, \underline{t}, \underline{r})$
2 $cK(\underline{t}, \underline{g}) = K(\underline{a}, \underline{t}, \underline{g})$ [12]
3 $cK(\underline{t}, \underline{b}) = K(\underline{a}, \underline{t}, \underline{b})$

4

5 for all \underline{t} — but usually represented only as a sampling of
6 e. g. roughly seventeen of the tonal values \underline{t} . This ex-
7 pression includes the previously defined scaling factor \underline{a}
8 that interrelates the overall ranges of the composite col-
9 or (here cK) and its constituent colors (here K).

10

11 (f) Ranging adjustment — The scaling factor \underline{a} is
12 necessary because of the range problem mentioned in sub-
13 section 2, "COMPLETE SAMPLING", above. Other, more com-
14 plex functions could be used, but a simple factor is
15 sufficient.

16 A single, unitary value of \underline{a} for use throughout the
17 system is found empirically. This is done by comparing
18 the darkest available data row in the composite-black (cK)
19 measurement tabulation 166 (Fig. 8) — namely, one-hundred
20 percent of all three primaries — with the full true-black
21 (K) measurement tabulation 168.

22 As demonstrated by the numerical example in the il-
23 lustration, higher percentages (\underline{t}) of true-black (K) ink
24 correspond to lower reflectance values C , M , Y . At the
25 bottom of the true-black tabulation 168, these reflectance
26 values approach zero.

27 The darkest available row in the composite-black (cK)
28 tabulation 166 typically is less dark (i. e. has a higher
29 reflectance value) than the true-black (K) tabulation 168,
30 in at least one column (C , M or Y). In the example, that
31 less-dark entry 167 is the magenta value "0.3712", which
32 is much higher than the true-black one-hundred-percent
33 entry "0.213"; and in fact also higher than the ninety-
34 percent magenta entry "0.2917".

1 From these observations it will now be clear that it
 2 would be fallacious to attempt to match one-hundred per-
 3 cent of composite black with one-hundred percent of true
 4 black. The maximum composite-black reflectance is even
 5 just slightly higher than the eighty-percent magenta value
 6 169, which appears as "0.3704".

7 This eighty-percent true-black entry 169, however, is
 8 a rather close match to the hundred-percent composite-
 9 black entry 167. Thus for purposes of the example the
 10 desired scaling factor may be set to $a = 0.8$ (i. e. eighty
 11 percent).

12 Those skilled in the field will appreciate that a
 13 more precise value of a if desired can be obtained either
 14 by iterated printing and measurement of a test pattern
 15 with finer resolution, or by interpolation. In any event,
 16 given the determined value of the scaling factor a , the
 17 next step is to complete the calibration.

18
 19 (g) Solution — Linking the above-stated "condition"
 20 with the composite-black model yields:

21
 22 $cK(\underline{t}, \underline{r}) = K(\underline{a}, \underline{t}, \underline{r}) = C(\underline{t}, \underline{r}) \cdot R(\underline{t}, \underline{r}) \cdot \beta_R(\underline{t})$
 23 $cK(\underline{t}, \underline{g}) = K(\underline{a}, \underline{t}, \underline{g}) = M(\underline{t}, \underline{g}) \cdot G(\underline{t}, \underline{g}) \cdot \beta_G(\underline{t})$ [13]
 24 $cK(\underline{t}, \underline{b}) = K(\underline{a}, \underline{t}, \underline{b}) = Y(\underline{t}, \underline{b}) \cdot B(\underline{t}, \underline{b}) \cdot \beta_B(\underline{t})$.

25
 26 Discarding the left-hand member of this three-way equality
 27 and substituting the previously determined modeling ex-
 28 pressions for the secondaries R, G, B —

29
 30 $K(\underline{a}, \underline{t}, \underline{r}) = C(\underline{t}, \underline{r}) \cdot M(\underline{t}, \underline{r}) \cdot Y(\underline{t}, \underline{r}) \cdot \alpha_R(\underline{t}) \cdot \beta_R(\underline{t})$
 31 $K(\underline{a}, \underline{t}, \underline{g}) = M(\underline{t}, \underline{g}) \cdot C(\underline{t}, \underline{g}) \cdot Y(\underline{t}, \underline{g}) \cdot \alpha_G(\underline{t}) \cdot \beta_G(\underline{t})$ [14]
 32 $K(\underline{a}, \underline{t}, \underline{b}) = Y(\underline{t}, \underline{b}) \cdot C(\underline{t}, \underline{b}) \cdot M(\underline{t}, \underline{b}) \cdot \alpha_B(\underline{t}) \cdot \beta_B(\underline{t})$.

33

1 Dividing through each of these remaining equations to
2 isolate C, M, Y produces these expressions for each pri-
3 mary as a function of desired tonal level — and the other
4 primaries:

5 $C(t, x) = \frac{K(a, t, x)}{M(t, x) \cdot Y(t, x) \cdot \alpha_R(t) \cdot \beta_R(t)}$

6 $M(t, g) = \frac{K(a, t, g)}{M(t, g) \cdot Y(t, g) \cdot \alpha_G(t) \cdot \beta_G(t)}$ [15]

7 $Y(t, b) = \frac{K(a, t, b)}{M(t, b) \cdot Y(t, b) \cdot \alpha_B(t) \cdot \beta_B(t)}$

8 This is the three-equation/three-variable system to be
9 solved.

10 As mentioned earlier, ultimately the variables to be
11 found are the numerical values of t_N (where N = R, G or B)
12 which the printing device must invoke to obtain desired
13 composite-black neutrality at some corresponding nominal
14 tonal value t_K of desired black.

15 These numerical values of t_N , however, are best
16 reached by finding their associated C, M and Y through
17 solution of the equations just above. Then, as also men-
18 tioned earlier, the needed t_N are simply inferred (read)
19 from the tabulation — with interpolation as appropriate.

20 In much of this discussion, various subindices have
21 been omitted to simply the presentation. It is now help-
22 ful, however, to display the above three expressions with
23 all the subindices more explicitly specified as follows.

24
25 //
26 //
27 //
28
29 //
30 //
31 //
32 //
33 //
34 //

$$\begin{aligned}
 1 & C(t_c, x) = \frac{K(a, t, x)}{M(t_M, x) \cdot Y(t_Y, x) \cdot \alpha_R \left(\frac{t_M + t_Y}{2} \right) \cdot \beta_R \left(\frac{t_c + \left(\frac{t_M + t_Y}{2} \right)}{2} \right)} \\
 2 \\
 3 \\
 4 \\
 5 \\
 6 & M(t_M, g) = \frac{K(a, t, g)}{C(t_c, g) \cdot Y(t_Y, g) \cdot \alpha_G \left(\frac{t_c + t_Y}{2} \right) \cdot \beta_G \left(\frac{t_M + \left(\frac{t_c + t_Y}{2} \right)}{2} \right)} \\
 7 \\
 8 \\
 9 \\
 10 & Y(t_Y, b) = \frac{K(a, t, b)}{M(t, b) \cdot Y(t, b) \cdot \alpha_B \left(\frac{t_c + t_M}{2} \right) \cdot \beta_B \left(\frac{t_Y + \left(\frac{t_c + t_M}{2} \right)}{2} \right)} \\
 11 \\
 12 \\
 13 \\
 14
 \end{aligned}$$

[16]

17 where: α , β are the model correction factors found or
18 estimated from the measured values, as exhibited
19 earlier.

20 t_c , t_M , t_Y are the tonal values (color percenta-
21 ges) of cyan, magenta and yellow — i. e., the
22 ultimately needed variables,

23 a is the rescaling factor,

24 t is the tonal value of the grayscale for which
25 t_c , t_m , t_y are sought,

26 K are true-black as measured from the test pat-
27 tern, and

28 C, M, Y are chromatic primaries, also as measured.

30 A way to complete the solution is iteratively — for in-
31 stance, first find the $C(t, \underline{r})$, given the initially mea-
32 sured M and Y . With this first-found value of $C(t, \underline{r})$, the
33 next step is to find (directly from the line-sensor data

1 as described above) the tonal value t_c of cyan that is
2 needed to provide a neutral gray.

3 Next the procedure goes to the next equation, the
4 equation for M, again using the initially measured Y but
5 now with the newly estimated C — and then to the third
6 equation, the equation for Y, now inserting both the new C
7 and M. This round is then iterated until values converge
8 to the desired accuracy.

9 The order of the equations can be changed to reach
10 convergence more quickly. In general the best sequence is
11 Y, then C and then M — but in practice the preferred or-
12 der depends on the particular ink set in use.

13
14 (h) Process summary — The foregoing discussion
15 shows that the invention is practiced by these steps:

17

1. print ramps (C, M, Y, R, G, B, cK, K),
2. measure ramps with each LED of sensor,
3. find scaling factor a from data,
4. set up model (α , β) with the sensor data,
5. find new C, M, Y from equations,
6. iterate to reach desired accuracy, and
7. find t_c , t_M , t_Y from data, for each C, M, Y.

24

25 (i) Fine tuning — The search can be further refined
26 if conducted in several printing passes, if there is a
27 need for finer accuracy. This iteration can be performed
28 in at least these ways:

29 The model pattern can be printed once again, but this
30 time all ramps are printed with the correction found in
31 the first effort — so that cK grays are closer to neutral
32 at the outset. The process then continues as before, and

1 the new color-correction values are linked with those
2 found in the first attempt.

3 Alternatively the complete-sampling and model-based
4 searches can be combined. Preferably the search is begun
5 with the modeling, to obtain gray-balancing functions as
6 above. Then taking the solutions as centerpoints, a com-
7 plete-sampling search is performed with very small incre-
8 ments, such as for example one percent.

9
10 (j) Contracted gamut — Modeling as described above
11 measures primaries and secondaries, i. e. fully saturated
12 colorants. This approach has the benefits of simplicity
13 and considering the full gamut.

14 The sampled space can be contracted transversely,
15 however, to probe at much finer resolution the region
16 nearest the gray axis. One way to implement this strategy
17 is to perform a simple change of base — in other words,
18 to define $C' = \underline{b}_c C$ (Fig. 9), $M' = \underline{b}_M M$, $Y' = \underline{b}_Y Y$, $R' = \underline{b}_R R$,
19 $G' = \underline{b}_G G$, $B' = \underline{b}_B B$.

20 The illustration is a diagram of CMY space. The sol-
21 id colored lines C , M , Y are the conventional orthogonal
22 axes, and the dashed colored lines C' , M' and Y' are modi-
23 fied axes which have been, so to speak, "shrunk" or con-
24 tracted — so that they are closer to the gray axis G ,
25 which appears as a solid gray line.

26 The parameter represented is how the axes are shrunk,
27 in terms of the angle of deviation. The angle of contrac-
28 tion is an angle in the plane that contains the primary
29 axis (e. g. C) under consideration and the gray axis G .

30 Orthogonal axes would be shrunk zero degrees, while
31 fully shrunk axes would be forty-five degrees. All values
32 intermediate between those are possible.

33
34

1 The change of base should be understood as very general;
2 hence the quantities \underline{b} are preferably vectors, or in the
3 alternative the change of base may be parametrized with \underline{b}
4 in order to contract more less (in which case \underline{b} may be
5 treated as scalar).

6 The several scaling vectors \underline{b} may be equal if pre-
7 ferred. On the other hand, if desired the new axes C', M'
8 and Y' (Fig. 9) can be parametrized to shrink more or less
9 depending on the kind of medium etc. for which the cali-
10 bration is to apply.

11 For $|\underline{b}| > 1$ the effect is to consider washes, i. e.
12 less-saturated mixtures, of the primaries and secondaries.
13 Secondaries furthermore are now the composition of the
14 newly defined primaries, e. g. $B' = C' + M'$.

15 The modeling equations described above are now ap-
16 plied in exactly the same way as with the conventionally
17 defined base. Once the solution is found, in terms of
18 C'M'Y', the inverse base change is applied to express the
19 results in terms of conventional CMY.

20
21

22 4. MECHANICAL AND PROGRAM/METHOD FEATURES

23

24 The invention is amenable to implementation in a
25 great variety of products. It can be embodied in a prin-
26 ter/plotter that includes a main case 1 (Fig. 10) with a
27 window 2, and a left-hand pod 3 which encloses one end of
28 the chassis. Within that enclosure are carriage-support
29 and -drive mechanics and one end of the printing-medium
30 advance mechanism, as well as a pen-refill station with
31 supplemental ink cartridges.

32 The printer/plotter also includes a printing-medium
33 roll cover 4, and a receiving bin 5 for lengths or sheets
34 of printing medium on which images have been formed, and

1 which have been ejected from the machine. A bottom brace
2 and storage shelf 6 spans the legs which support the two
3 ends of the case 1.

4 Just above the print-medium cover 4 is an entry slot
5 7 for receipt of continuous lengths of printing medium 4.
6 Also included are a lever 8 for control of the gripping of
7 the print medium by the machine.

8 A front-panel display 211 and controls 212 are moun-
9 ted in the skin of the right-hand pod 213. That pod en-
10 closes the right end of the carriage mechanics and of the
11 medium advance mechanism, and also a printhead cleaning
12 station. Near the bottom of the right-hand pod for readi-
13 est access is a standby switch 214.

14 Within the case 1 and pods 3, 213 a cylindrical plat-
15 en 241 (Fig. 11) — driven by a motor 242, worm and worm
16 gear (not shown) under control of signals from a digital
17 electronic processor 71 — rotates to drive sheets or
18 lengths of printing medium 4A in a medium-advance direc-
19 tion. Print medium 4A is thereby drawn out of the print-
20 medium roll cover 4.

21 Meanwhile a pen-holding carriage assembly 220 (Figs.
22 11 and 12) carries several pens 223-226 (Fig. 11) back and
23 forth across the printing medium, along a scanning track
24 — perpendicular to the medium-advance direction — while
25 the pens eject ink. As mentioned earlier, this is one but
26 not the only form of incremental-printing apparatus, an
27 alternative being use of a page-wide pen array with rela-
28 tive motion in relation to the full length of the printing
29 medium. (As will be understood, the term "scan" is also
30 used in describing motion of a measuring sensor over the
31 printing medium, most usually along the medium-advance
32 direction.)

33 For simplicity's sake, only four pens are illustra-
34 ted; however, as is well known a printer may have six pens

1 or more, to hold different colors — or different dilu-
2 tions of the same colors — as in the more-typical four
3 pens. The medium 4A thus receives inkdrops for formation
4 of a desired image, and is ejected into the print-medium
5 bin 5. A colorimetric image sensor 251, quite small,
6 rides on the carriage with the pens.

7

8 A very finely graduated encoder strip 233, 236 (Fig.
9 12) is extended taut along the scanning path of the car-
10 riage assembly 220 and read by another small automatic
11 optoelectronic sensor 237 to provide position and speed
12 information 237B for the microprocessor. One advantageous
13 location for the encoder strip is shown in several of the
14 earlier cross-referenced patent documents at 236, immedi-
15 ately behind the pens.

16 A currently preferred position for the encoder strip
17 233 (Fig. 11), however, is near the rear of the pen-car-
18 riage tray — remote from the space into which a user's
19 hands are inserted for servicing of the pen refill car-
20 tridges. For either position, the encoder-strip sensor
21 237 is disposed with its optical beam passing through
22 orifices or transparent portions of a scale formed in the
23 strip.

24 The pen-carriage assembly 220, 220' (Figs. 11 and 12)
25 is driven in reciprocation by a motor 231 — along dual
26 support and guide rails 232, 234 — through the intermedi-
27 ary of a drive belt 235. The motor 231 is under the con-
28 trol of signals from digital processors 71.

29 Naturally the pen-carriage assembly includes a for-
30 ward bay structure 222 for the pens — preferably at least
31 four pens 223-226 holding ink of four different colors
32 respectively. Most typically the inks are yellow in the
33 leftmost pen 223, then cyan 224, magenta 225 and black
34 226. As a practical matter, chromatic-color and black

1 pens may be in a single printer, either in a common car-
2 riage or plural carriages.

3 Also included in the pen-carriage assembly 220, 220'
4 is a rear tray 221 carrying various electronics. Figs. 10
5 and 11 most specifically represent a system such as the
6 Hewlett Packard printer/plotter model "DesignJet 1000",
7 which product does not include the present invention.
8 These drawings, however, also illustrate certain embodi-
9 ments of the invention, and — with certain detailed dif-
10 ferences mentioned below — a printer/plotter that in-
11 cludes preferred embodiments of the invention.

12
13 Before further discussion of details in the block
14 diagrammatic showing of Fig. 12, a general orientation to
15 that drawing may be helpful. Most portions 70, 73-78, 66
16 across the lower half of the diagram, including most 4A-
17 251 of the printing stage at far right, are generally con-
18 ventional and represent the context of the invention in an
19 inkjet printer/plotter.

20 The top portion 62-65, 80-85 of the drawing and
21 certain parts 251', 251" of the printing stage represent
22 the present invention. Given the statements of function
23 presented in this document, an experienced programmer of
24 ordinary skill in this field can prepare suitable programs
25 for operation of all the circuits.

26
27 The pen-carriage assembly is represented separately
28 at 220 when traveling to the left 216 while discharging
29 ink 218, and at 220' when traveling to the right 217 while
30 discharging ink 219. It will be understood that both 220
31 and 220' represent the same pen carriage.

32 The previously mentioned digital processor 71 pro-
33 vides control signals 220B to fire the pens with correct
34 timing, coordinated with platen drive control signals 242A

1 to the platen motor 242, and carriage drive control sig-
2 nals 231A to the carriage drive motor 231. The processor
3 71 develops these carriage drive signals 231A based partly
4 upon information about the carriage speed and position
5 derived from the encoder signals 237B provided by the
6 encoder 237.

7 (In the block diagram almost all illustrated signals
8 are flowing from top toward bottom and left toward right.
9 The exceptions are the information 237B fed back from the
10 codestrip sensor 237, the image-reflectance measurement
11 profile data 65 fed back from the colorimetric sensor 251,
12 and the scaling information 172 — all as indicated by the
13 associated leftward arrows.)

14 The codestrip 233, 236 thus enables formation of col-
15 or inkdrops at ultrahigh precision during scanning. This
16 precision is maintained in motion of the carriage assembly
17 220 in each direction — i. e., either left to right (for-
18 ward 220') or right to left (back 220).

19 New image data 70 are received 191 into an image-
20 processing stage 73, which may conventionally include a
21 contrast and color adjustment or correction module 76 and
22 rendition and scaling modules 74, 77, 77'. Most commonly,
23 scaling (if any) is performed in conjunction with rendi-
24 tion 75.

25 Information 193 passing from the image-processing
26 module 73 next enters a printmasking module 76. This gen-
27 erally includes a stage 77 for specific pass and nozzle
28 assignments.

29 Integrated circuits 71 may be distributive — being
30 partly in the printer, partly in an associated computer,
31 and partly in a separately packaged raster image proces-
32 sor. Alternatively the circuits may be primarily or whol-
33 ly in just one or two of such devices.

1 These circuits also may comprise a general-purpose
2 processor (e. g. the central processor of a general-pur-
3 pose computer) operating software such as may be held for
4 instance in a computer hard drive, or operating firmware
5 (e. g. held in a ROM 75 and for distribution 66 to other
6 components), or both; and may comprise application-spe-
7 cific integrated circuitry. Combinations of these may be
8 used instead.

9
10 As set forth above, images to be printed and scanned
11 to establish the modifications prescribed by the present
12 invention may be representative area-fill images of dif-
13 ferent colors, for reading by the optical sensor 251 to
14 generate calibration data. For generation of such test
15 images, the apparatus of the invention includes — in the
16 integrated-circuit section 71 (Fig. 12) — printing means
17 62 that generate control signals 80 for operation of the
18 final output stage 78. These signals drive the printing
19 stage seen at right.

20 In addition to the simple formatting instructions
21 necessary merely to define a geometrical pattern of test
22 patches 101, 111, 121-25, 131-35 (Fig. 1) — or alterna-
23 tively 171-74, 176-79 (Fig. 4) — the control signals 80
24 include a series of different colorimetric parameters for
25 test, as appropriate for establishing the multiple colors
26 of the patches respectively.

27 Such a series of parameters typically defines the
28 colorant deposition corresponding to the nominal ramp
29 colors, and in the case of the sampling method of Fig. 1
30 also includes a sequence of subtly differing color com-
31 mands defining the variations about each nominal color.
32 Each value is duly implemented by the final output stage
33 78 and its output signals 220B, 231A, 242A. These signals
34 are further implemented, in printing of the test images,

1 by the movements of the advance motor 242, drive 241 and
2 medium 4A.

3

4 A small automatic optoelectronic sensor 251 rides
5 with the pens on the carriage and is directed downward to
6 obtain data about color. More specifically, the sensor
7 measures color in the test patches, for purposes of the
8 adjustments set forth earlier in this document.

9 Ramp-measurement interpreting means 82 receive meas-
10 urement data 65 returned from the sensor 251. In the case
11 of the optimization embodiments, these interpreting means
12 82 include means for correlating these colorimetric data
13 65 with the phase of the waveband-selection signals 87 as
14 well as the colorimetric components of the previously
15 discussed output-stage control signals 80.

16 Based upon the colorimetric data 65 and correlations,
17 the ramp-measurement interpreting means 82 generate sig-
18 nals 83 for controlling the compensation means 84 — which
19 in turn produce signals 86 that adjust the otherwise gen-
20 erally conventional color-correction module 74. Through
21 refined cooperation of these several modules, the compen-
22 sation means 84 are able to minimize chroma in nominally
23 neutral image features — and also, as explained earlier,
24 to trim up the reproduction of color throughout the gamut
25 of the printing device.

26 More specifically, the compensation means 84 include
27 a calculation stage 85 that reduces chroma to roughly 2.5
28 ΔE or less. The notation ΔE represents color difference
29 in three-dimensional color space, particularly the percep-
30 tual CIELA*B* space.

31 As set forth in other patent documents, the same or
32 related data 65 can be used for control of other parame-
33 ters. These may include printmode; print-medium advance

1 speed and stroke; scan velocity; inkdrop energies, sizes
2 and velocities; depletion, propletion and discretionary-
3 dotting ratios; balance point between randomization vs.
4 granularity; and also nozzle weighting distributions.

5

6 The sensor 251 signals are coordinated (not shown)
7 with movements of the carriage and advance mechanism
8 during sensing. These signals are also coordinated with
9 operation of ramp-measurement controlling means 81 that
10 generate — among other control information — signals 87
11 for controlling the lamps 251' (Fig. 12) or wavelength-
12 differentiation unit 88 (Fig. 13).

13 In particular the lamps 251' advantageously take the
14 form of red, green and blue light-emitting diodes (LEDs)
15 R, G, B respectively. These diodes are energized by their
16 control signals 87 to produce specifically timed light
17 pulses 251" for illuminating the test pattern (Fig. 1 or
18 4) on the printing medium 4A — and thereby reflecting
19 light in specified wavebands into the sensor 251.

20 This enables discrimination of the reflected colors
21 as discussed earlier. In practice the lamps 251' are typ-
22 ically mounted within the housing of the sensor 251, and
23 thus are carried transversely across the printing medium
24 4A by the carriage 220 — as motivated 235 by the motor
25 231 and its control signals 231A. Propagation of the
26 light pulses 251" to the printing medium accordingly is
27 almost completely within the protected environment of the
28 sensor housing.

29

30 In an alternative illumination and sensing arrange-
31 ment, the light source is instead a broadband single
32 source 251'BB (Fig. 13), which emits broadband light
33 251"BB toward the test pattern on the medium 4A. In the
34 illustrated arrangement this light is allowed to illumi-

00000000000000000000000000000000

1 nate the test pattern, and the reflected light passes to a
2 wavelength differentiator 88.

3 The latter may be a controlled filter set (e. g. with
4 a rotating chopper), or a controlled birefringent disper-
5 sive device, or a controlled diffractive unit, or any
6 other module that spatially, temporally and/or absorp-
7 tively, or otherwise separates illumination from the spec-
8 tral bands of interest, within the broadband illumination
9 251"BB. Selected light 251"S passes to the sensor 251.

10 To establish which waveband is being received by the
11 sensor 251, or by particular elements within the sensor
12 251, the differentiator 88 is controlled by the signals 87
13 from the ramp-measurement controlling means 81. The sen-
14 sor signals 65 proceed as before to the interpreting means
15 82. In another alternative configuration the differentia-
16 tor 88 is located at a suitable point 89 in the illumina-
17 tion path.

18
19 Any of these versions of the illumination and sensing
20 subsystem thereby readily performs optical measurements
21 65, 82 (Fig. 12) of the printed test images. Suitable
22 algorithmic control is well within the skill of the art,
23 guided by the discussions here.

24
25 Method aspects of the invention may be conceptualized
26 as preferably including five distinct major steps 301,
27 302, 311, 321 and 331 (Fig. 14). All these operate auto-
28 matically, and as will be understood such operation may
29 begin with reading instructions 66 out of a nonvolatile
30 memory 72 (Fig. 12) for control of the several integrated-
31 circuit modules. To the extent that some functions may be
32 effected in an ASIC, however, no such reading step is
33 required as such; simply powering up the circuit initiates

1 operation of whatever functions the unit has been con-
2 structed to perform.

3 The first major function 301 includes using the
4 printing device to print a gray ramp with a single black
5 ink. In the secondary-calibrating variant or aspect of
6 the invention, actual red, green or blue ink may be used
7 instead.

8 The second major function 302 includes using the same
9 device to print a nominally gray ramp with composite-black
10 ink — or, for a secondary-calibrating facet or variant,
11 with two-primary nominal approximations to the desired
12 secondaries. This major step 302 is then followed by a
13 further major step 311 of automatically measuring and com-
14 paring the two ramps.

15 Next is a fourth major step 321 of employing the
16 measured black ramp as a standard to correct the measured
17 composite-black ramp — and this preferably includes a
18 chroma-correction operation 322. A fifth such step 331
19 includes using the compared ramps to also correct other
20 colors.

22 The two main methods of practicing the present invention
23 are sampling 303-307, 322-325 and modeling 312-316,
24 326, 327. These alternatives are seen in the illustration
25 as two coordinated subchannels — to the left and right
26 respectively.

27 In particular, if sampling is favored then the print-
28 ing step 302 involves not only printing of a unitary com-
29 posite-black ramp as in the modeling case, but also the
30 substep 303 of printing plural nonblack combinations for
31 each gray tone to be calibrated.

32 Preferably this plural-combination printing substep
33 303 includes enough surrounding values to bracket 304 each
34 nominal value — and this in turn preferably includes op-

1 timizing 305 the bracketing, which optimizing itself pref-
2 erably includes printing combinations that surround 306
3 the nominal value in color space.

4 When this approach is employed, then after the major
5 measuring-and-comparing step 311, the employing step 321
6 is coordinated 307 with the printing substeps 303-306 by
7 the particular form 323 of the chroma-correction substep
8 322. More specifically, either the measured nonblack com-
9 binations are searched 324 to find one of those combina-
10 tions for use, or the system interpolates 325 among meas-
11 ured combinations — typically those which most closely
12 surround the target true gray.

13

14 If instead modeling is employed, then the plural non-
15 black-combination printing 303 is omitted — but when it
16 is time for measurement and comparison 311, a new step of
17 inserting 312 the measured values into equations is per-
18 formed. It is this step 312, rather than the "particular
19 form" 323 mentioned in the preceding paragraph, which is
20 then linked 316 to a specialized substep 326 in the em-
21 ploying step 321 — namely, the substep of solving the
22 equations to get the correction values for later use.

23 In the modeling case, the value-insertion substep 312
24 preferably includes using 313 expressions of the form pre-
25 sented in equation [1], [1'] earlier — and these expres-
26 sions in turn preferably take 314, 315 the special forms
27 that are described in the text immediately following equa-
28 tion [1']. As also noted earlier, the solution 326 is ad-
29 vantageously performed by iteration 327 of the equations.

30

31 As mentioned earlier, however, the sampling and mod-
32 eling regimens may be hybridized in various ways. One
33 particularly effective strategy for doing so is first to
34 go through the Fig. 14 method using the modeling options

1 in the right-hand channel 312-316, 326, 327 to very close-
2 ly narrow the field of search — ideally with iteration as
3 discussed above — and then to perform one or more final
4 rounds of search using the left-hand channel 302-307, 323.

5
6
7

8 The above disclosure is intended as merely exemplary,
9 and not to limit the scope of the invention — which is to
10 be determined by reference to the appended claims.